

# Compact Routing on Internet-Like Graphs

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# The motivation

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- # BGP routing table size scalability concerns: immediate causes are well studied (multihoming, more peering, traffic engineering, address allocation, etc.), but...
- # Typical “solution”: aggregate using (multiple) levels of *hierarchical network partitioning* in the Kleinrock-Kamoun style, but...
  - This scheme does not work for densely connected networks, so:

# The research problem

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- # **What are the *fundamental* scalability limits (in terms of routing table size) for routing?**
- # Recall, *stretch* is defined as:
  - $S = \max[(\text{hop count using routing scheme}) / (\text{shortest path in graph})]$
- # Fact: modern “compact routing” schemes can guarantee small routing table sizes. The price is increased maximum stretch, but...
- # Low ( $\sim 1$ ) stretch may well be a requirement for Internet routing, so: **What is the average stretch produced by these schemes on Internet-like [*scale-free*] topologies?**

# Stretch/local memory Results

- # Trivial shortest path  $\Rightarrow O(n \log n)$
- #  $1 \leq s < 1.4 \Rightarrow \Omega(n \log n)$  (*Gavoille/Perennes 96*)
- #  $1.4 \leq s < 3 \Rightarrow \Omega(n)$  (*Gavoille/Genegler 01*)
- #  $3 \leq s < 5 \Rightarrow O(n^{1/2} \log n)$  (*Eilam/Gavoille/Peleg 98*)
- # Thorup & Zwick (TZ01):  $s=3$ ,  $\Omega(n^{1/2} \log^{1/2} n)$ 
  - Improves over  $s=3$ ,  $O(n^{2/3} \log^{4/3} n)$  (*Cowen 99*)
  - Nearly “optimal,” up to logarithmic factor
  - The basis for our studies
  - (uses custom node labels; not a dynamic scheme)

# Our Approach

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- # Analysis: evaluate average TZ stretch as a function of the first two moments of an (assumed Gaussian) distance distribution in a graph
- # Simulations: develop a TZ simulator and use it on uncorrelated random power-law graphs (generated by PLRG) with node degree  $k$  ( $P_k \sim k^{-\gamma}$ ), and on classical random graphs

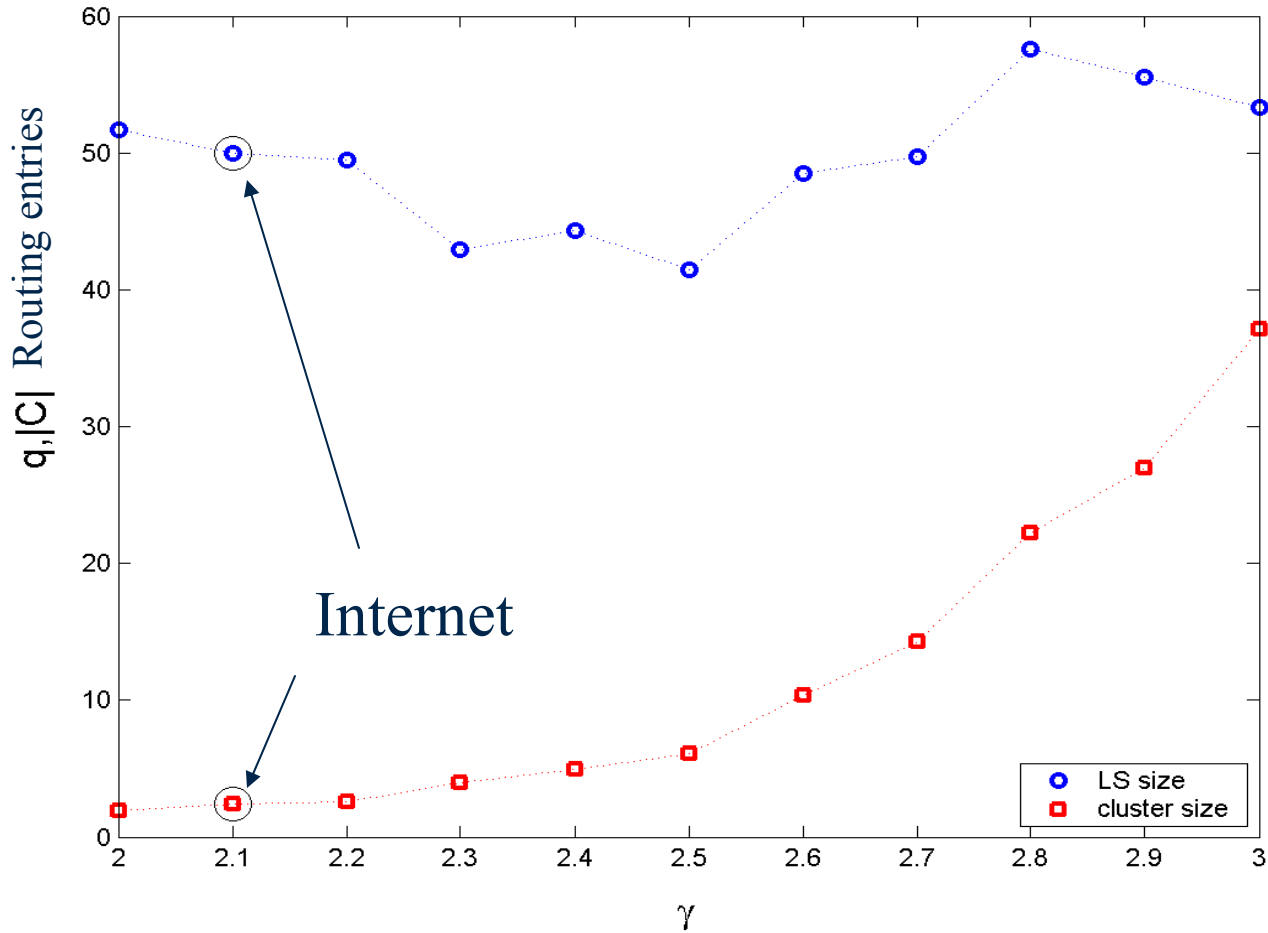
# Our Results

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Findings (analysis + simulations agree)

- # Routing table sizes are *well below* the theoretical upper bounds (52 vs. 2187 for  $n=10,000$ )
- # Average stretch:
  - is low ( $\sim 1.1$ ,  $\sim 70\%$  paths are shortest [stretch-1])
  - does not depend on the power-law exponent  $\gamma$
  - *decreases* with  $n$  (i.e. weak neg. correlation on  $n$ )
- # Remarkably, the average stretch function has a *unique critical point* and the Internet is located in its close neighborhood

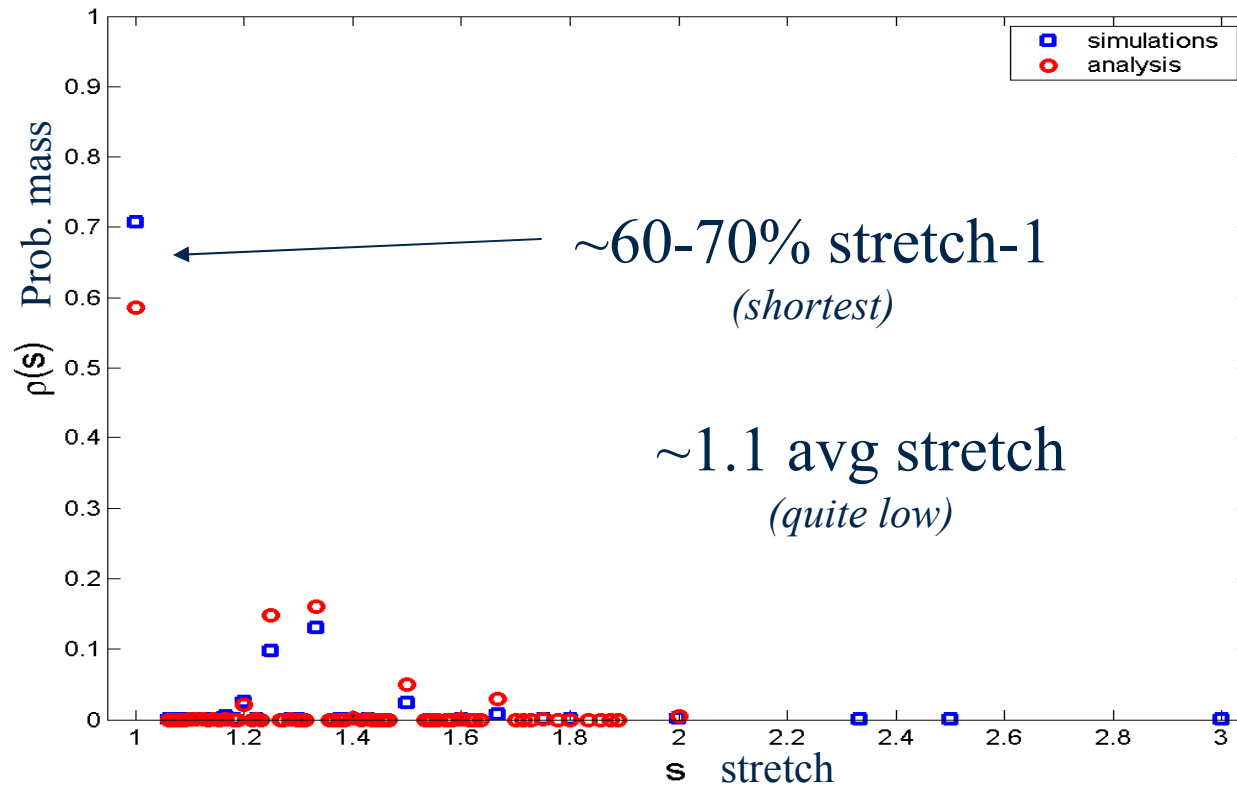
# Routing table sizes are small



# Stretch distribution / average

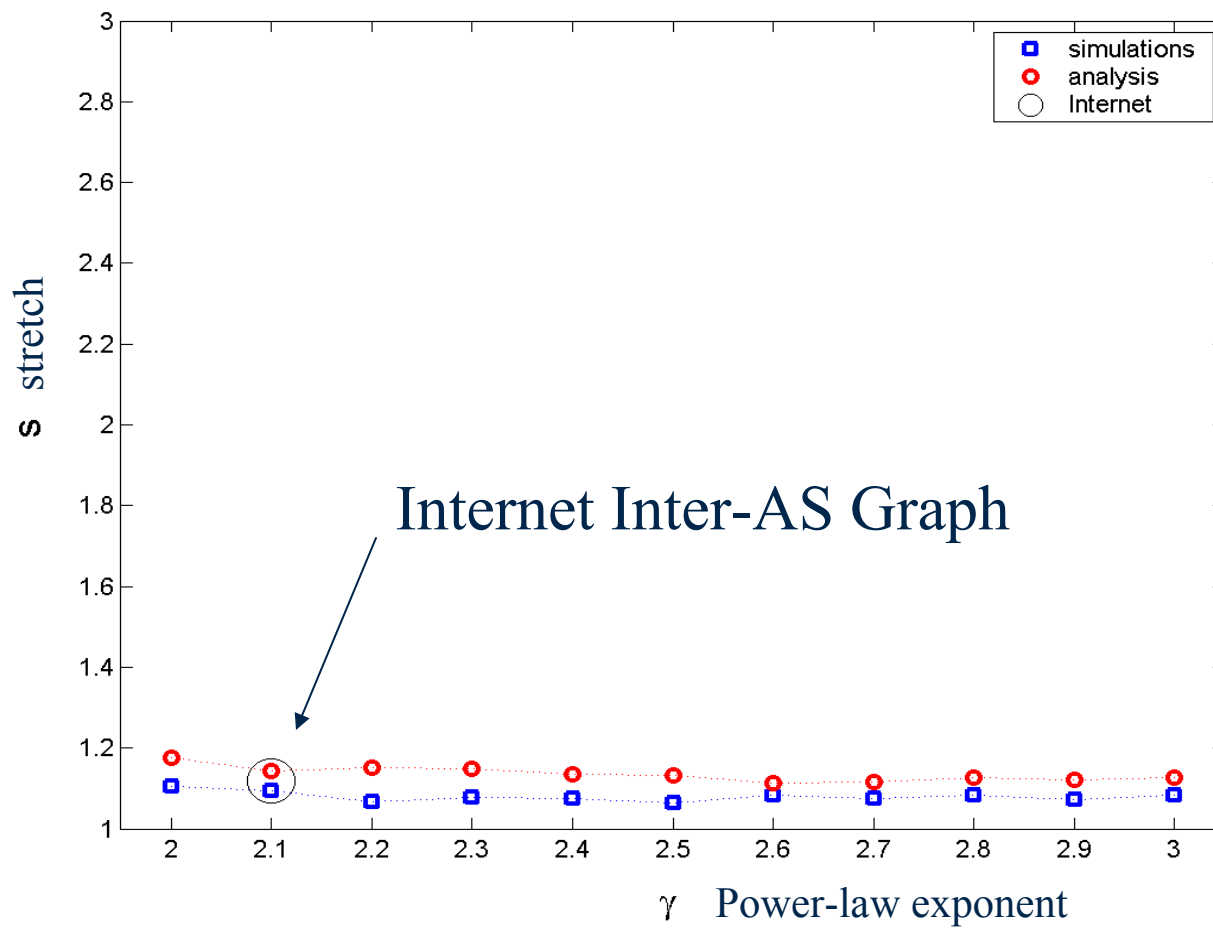
average  $s = 1.09$  (simulations, 10k nodes)  $\square$

average  $s = 1.14$  (analysis, DGM model)  $\circ$

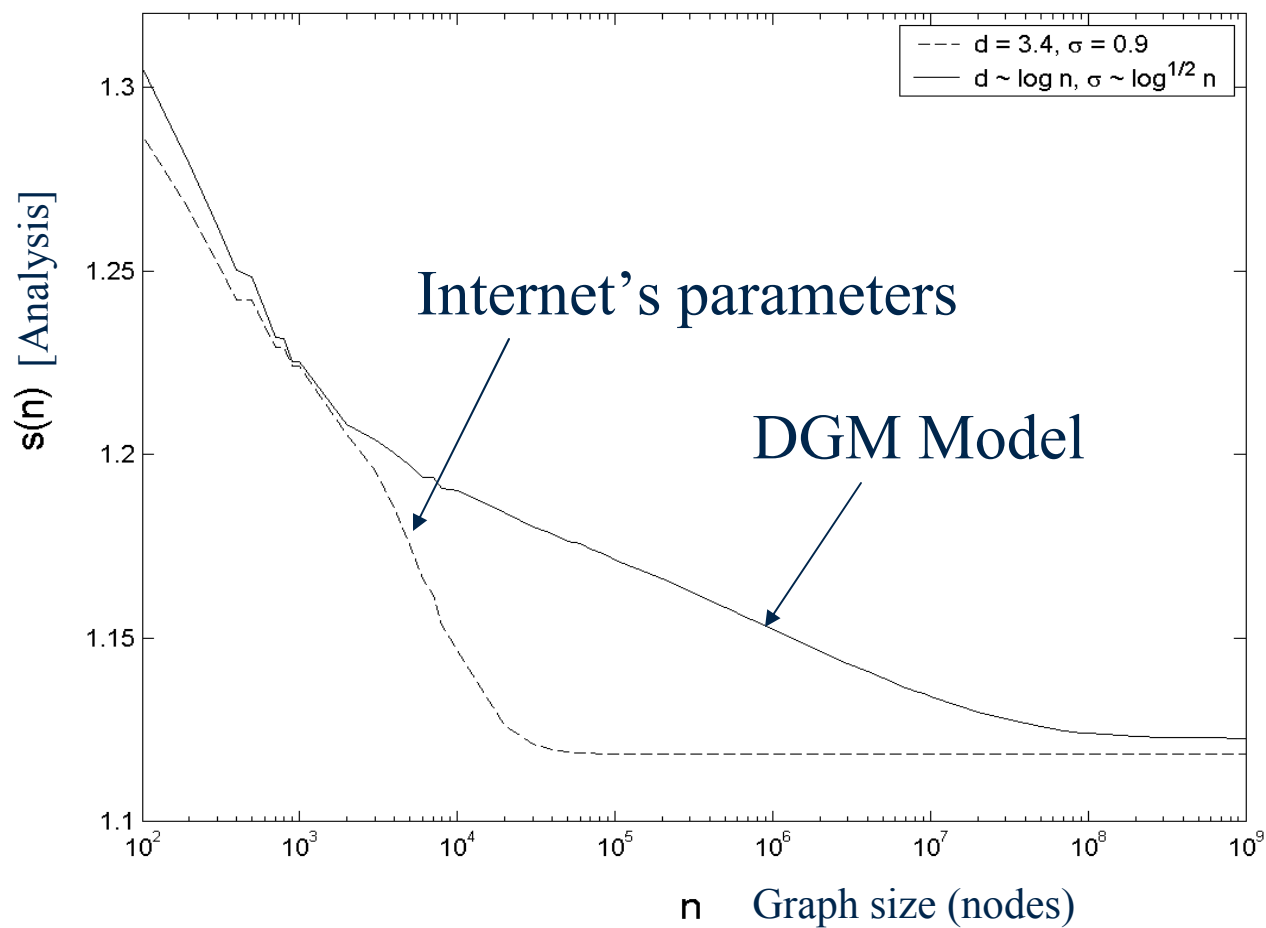




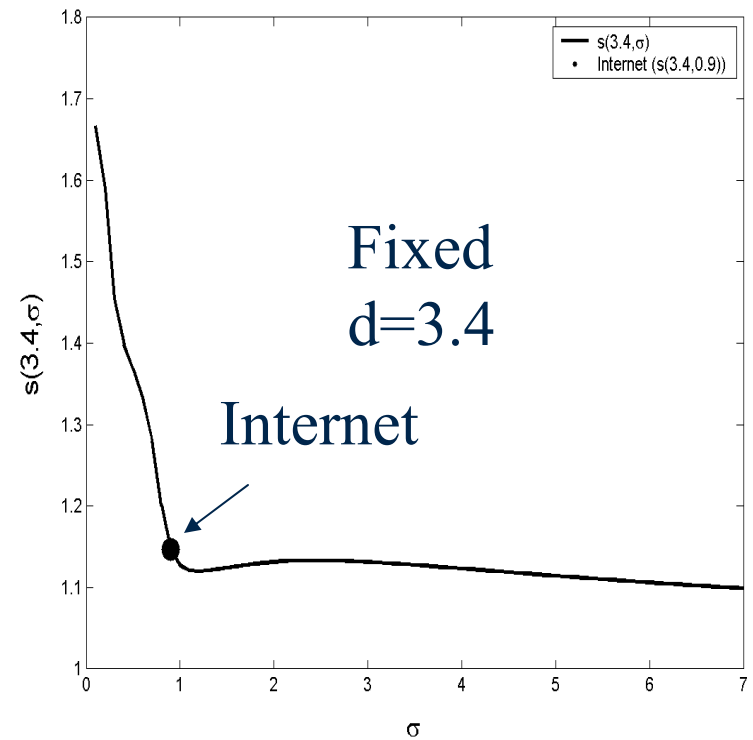
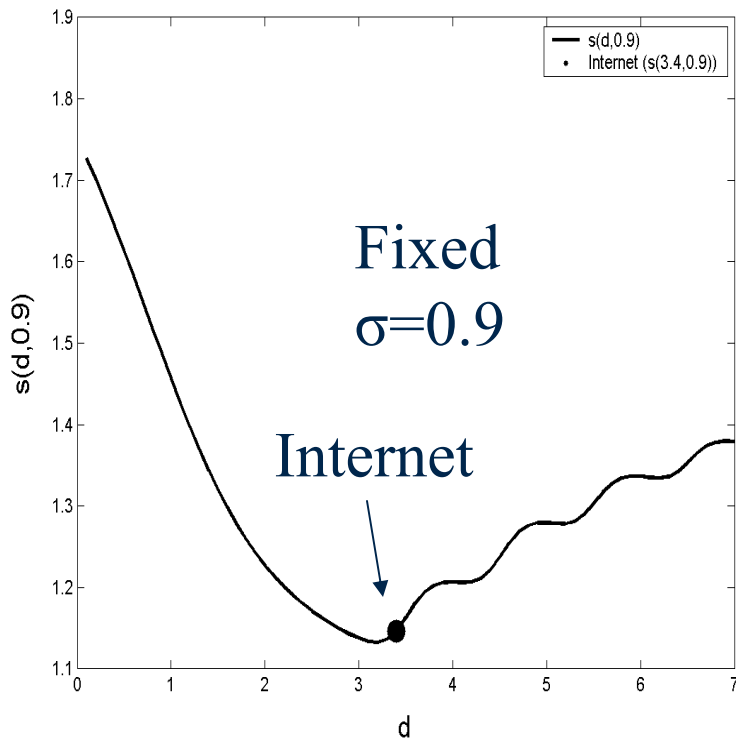
# Independence of $\gamma$ (n:10000)



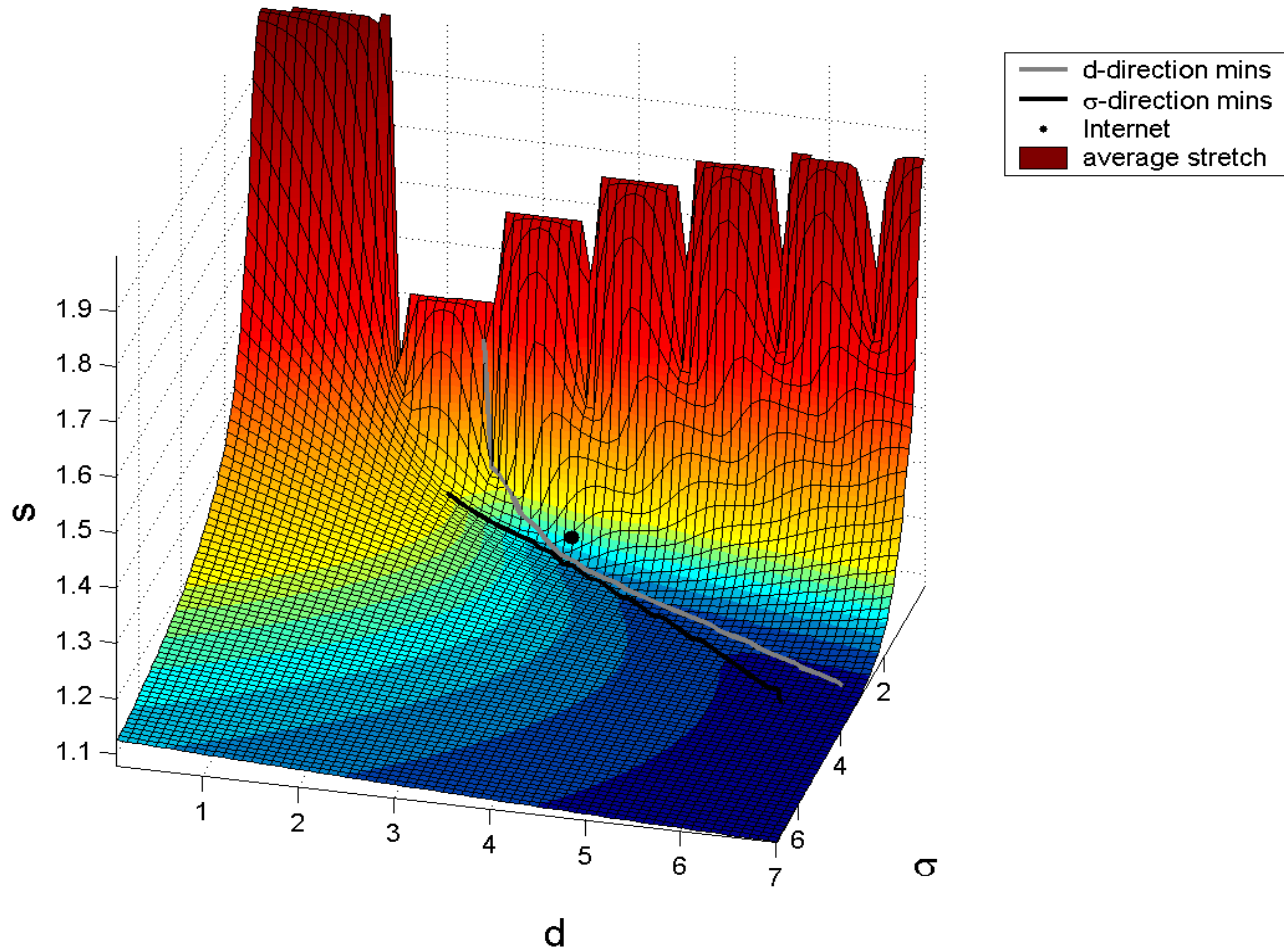
# $S$ Decreases with network size



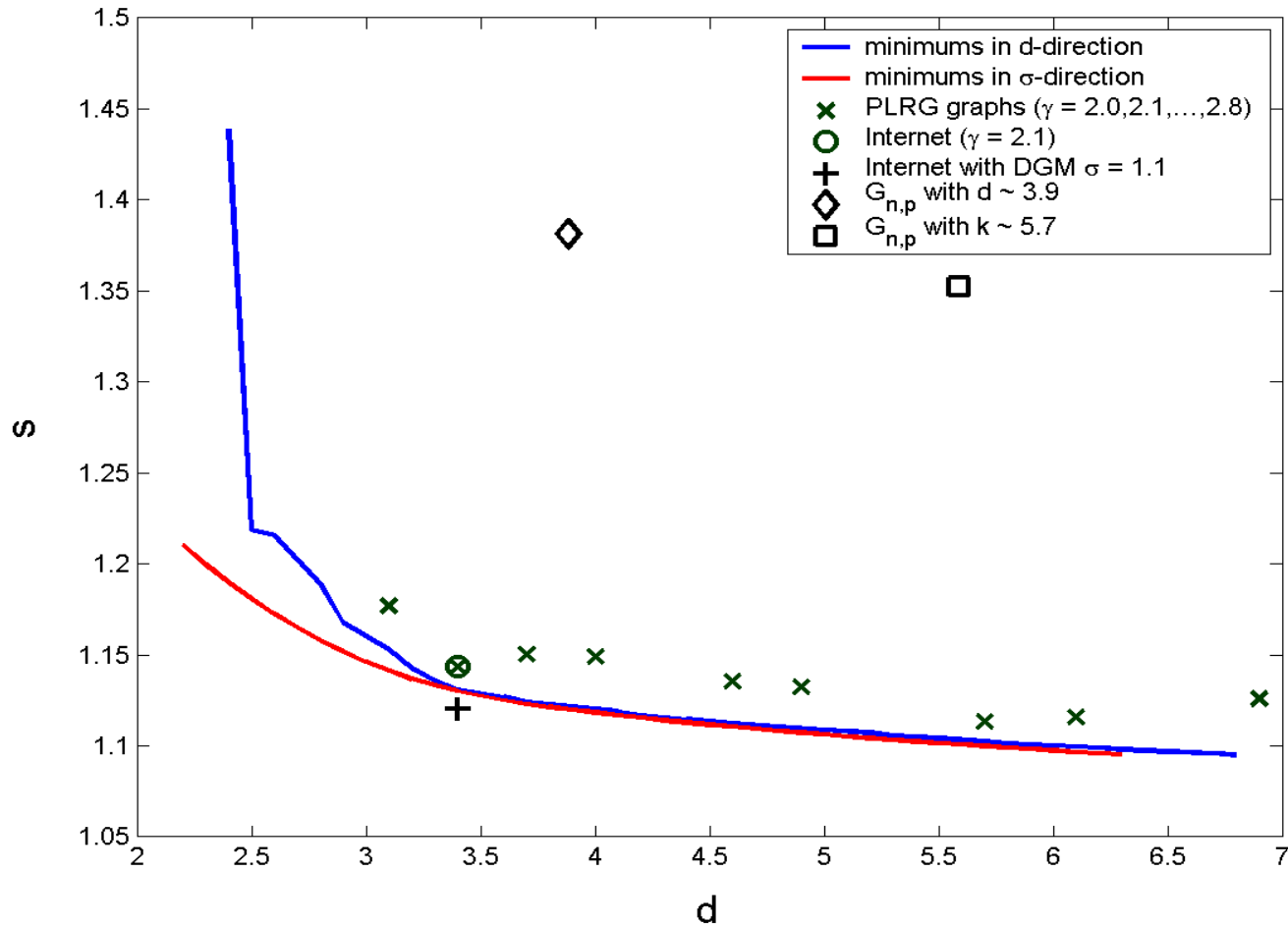
# Avg Stretch Dependency on $d, \sigma$ : Internet point $\sim$ minimizes stretch



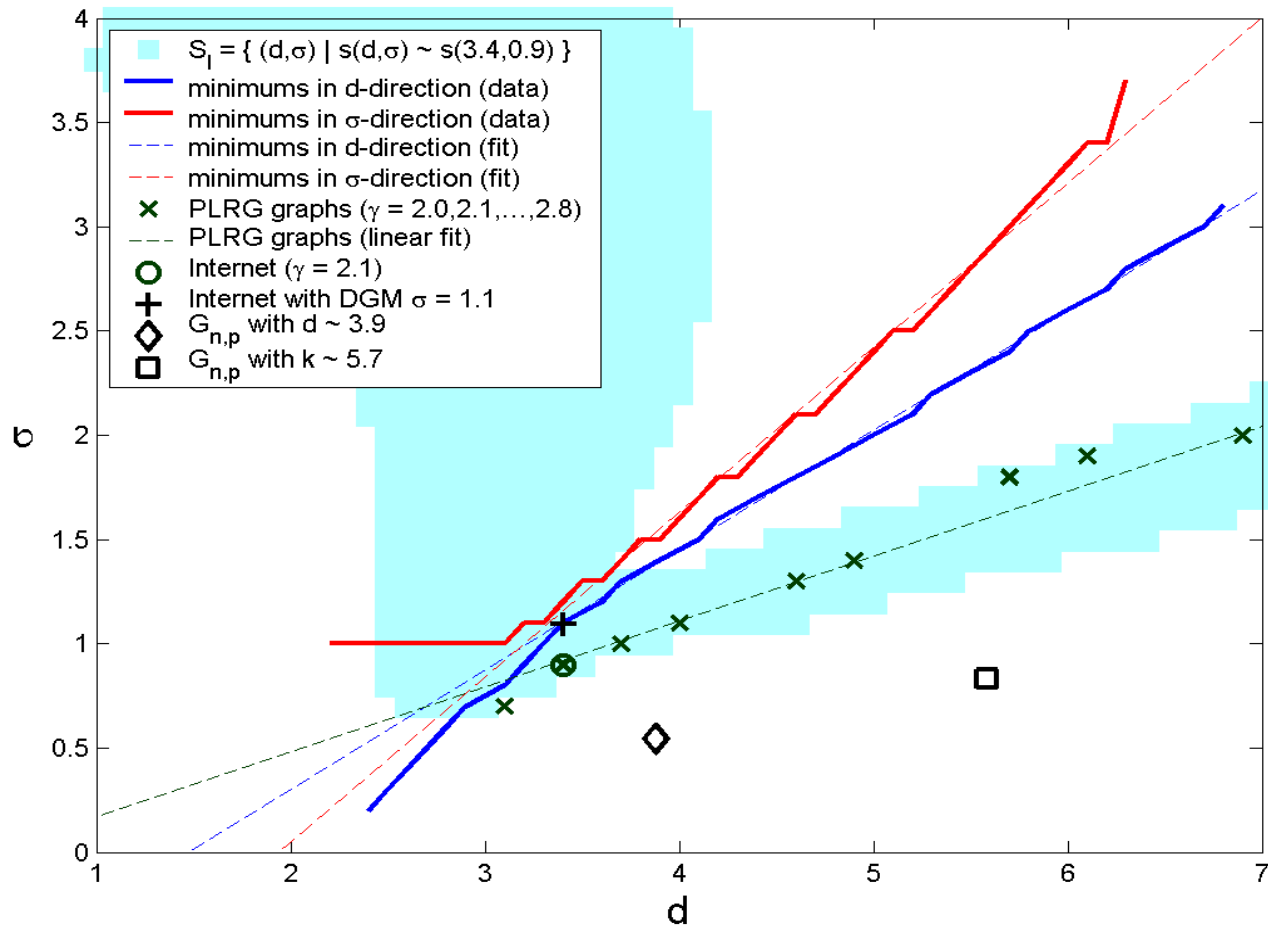
# TZ Stretch function (3d)



# Stretch function (d-s plane)



# Stretch function (d- $\sigma$ plane)



# Summary

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- # Fundamental limits to routing table size scalability
  - Compact routing (TZ scheme):
    - + *bounded stretch, small table sizes*
    - + *appears to work very well on scale-free graphs*
    - - *not yet a dynamic routing scheme, not stretch-1*
- # Internet point ~ quasi-stationary point
  - Stretch function may reveal drivers of Internet topology evolution
  - Need better understanding to know why



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Thank you!